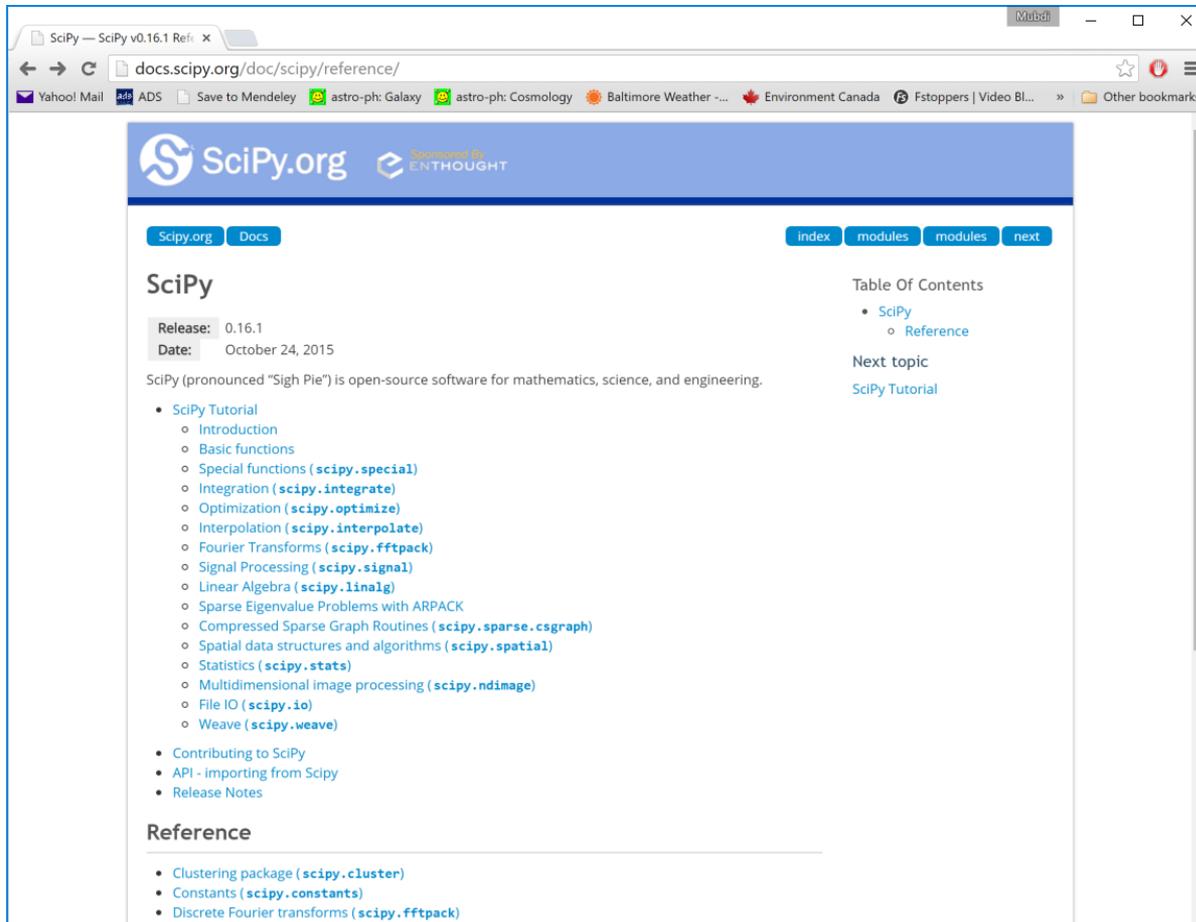


# 5. ADVANCED DATA TECHNIQUES

**JHU Physics & Astronomy**  
**Python Workshop 2017**

Lecturer: Mubdi Rahman

# SCIPY: FUNCTIONS YOU WANT, THE PACKAGE YOU NEED



The screenshot shows a web browser window displaying the SciPy v0.16.1 reference documentation. The page features the SciPy.org logo and the ENTHOUGHT logo. The main content area is titled "SciPy" and includes the following information:

- Release: 0.16.1
- Date: October 24, 2015
- SciPy (pronounced "Sigh Pie") is open-source software for mathematics, science, and engineering.
- Table of Contents
  - SciPy
    - Reference
- Next topic: SciPy Tutorial

The main content area lists various SciPy modules and their sub-modules:

- SciPy Tutorial
  - Introduction
  - Basic functions
  - Special functions (`scipy.special`)
  - Integration (`scipy.integrate`)
  - Optimization (`scipy.optimize`)
  - Interpolation (`scipy.interpolate`)
  - Fourier Transforms (`scipy.fftpack`)
  - Signal Processing (`scipy.signal`)
  - Linear Algebra (`scipy.linalg`)
  - Sparse Eigenvalue Problems with ARPACK
  - Compressed Sparse Graph Routines (`scipy.sparse.csgraph`)
  - Spatial data structures and algorithms (`scipy.spatial`)
  - Statistics (`scipy.stats`)
  - Multidimensional image processing (`scipy.ndimage`)
  - File IO (`scipy.io`)
  - Weave (`scipy.weave`)
- Contributing to SciPy
- API - Importing from SciPy
- Release Notes

The "Reference" section lists the following modules:

- Clustering package (`scipy.cluster`)
- Constants (`scipy.constants`)
- Discrete Fourier transforms (`scipy.fftpack`)

The Docs: <http://docs.scipy.org/doc/scipy/reference/>

# L.J. DURSI'S FIRST RULE OF PROGRAMMING

## Rule #1: Don't code!

For most common algorithms or problems that exist, there are functions and modules that have been optimized and tested by large groups of people who know what they're doing. Use these rather than programming your own.

Scipy has a lot of these functions and algorithms ready for your use. In this lesson, we'll go through a few of these useful functions.

# ORGANIZATION OF PACKAGES

## Scipy

Optimize/Fitting  
(`scipy.optimize`)

Integration  
(`scipy.integrate`)

Image Processing  
(`scipy.ndimage`)

Linear Algebra  
(`scipy.linalg`)

Statistics  
(`scipy.stats`)

Much More...

# INTERPOLATION

Importing the Functions:

```
from scipy import interpolate
```

Basic one-dimensional interpolation:

```
funct1 = interpolate.interp1d(  
xvals, yvals, kind='linear', bounds_error=False,  
fill_value=np.nan)
```

Kind options: 'linear', 'nearest', 'zero', 'slinear', 'quadratic', 'cubic'

# INTERPOLATION

Importing the Functions:

```
from scipy import interpolate
```

Basic one-dimensional interpolation:

```
funct1 = interpolate.interp1d(  
x, y, kind='linear', bounds_error=False,
```

## PRO TIP:

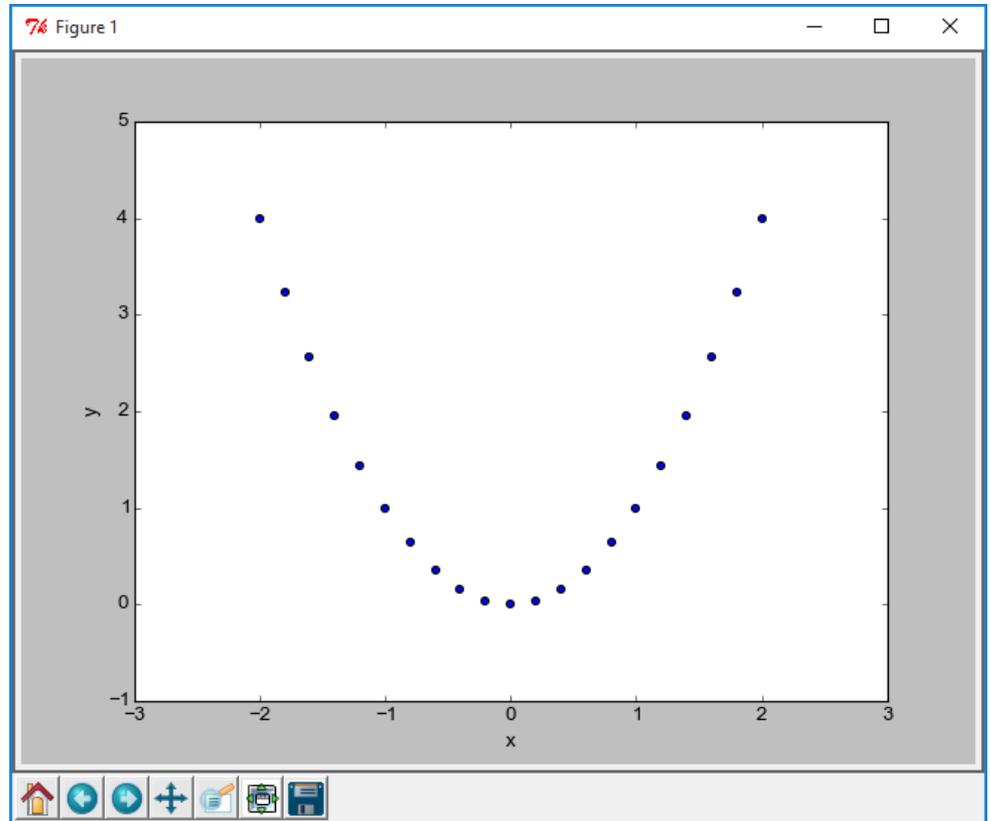
By default, the interpolation will fail if you go beyond the minimum and maximum points. The `bounds_error` keyword helps deal with this.

'zero', 'slinear', 'quadratic', 'cubic'

# INTERPOLATION

Given a simple function:

```
funct1 =  
interpolate.interp1d(  
    xvals, yvals,  
    kind='nearest'  
)
```

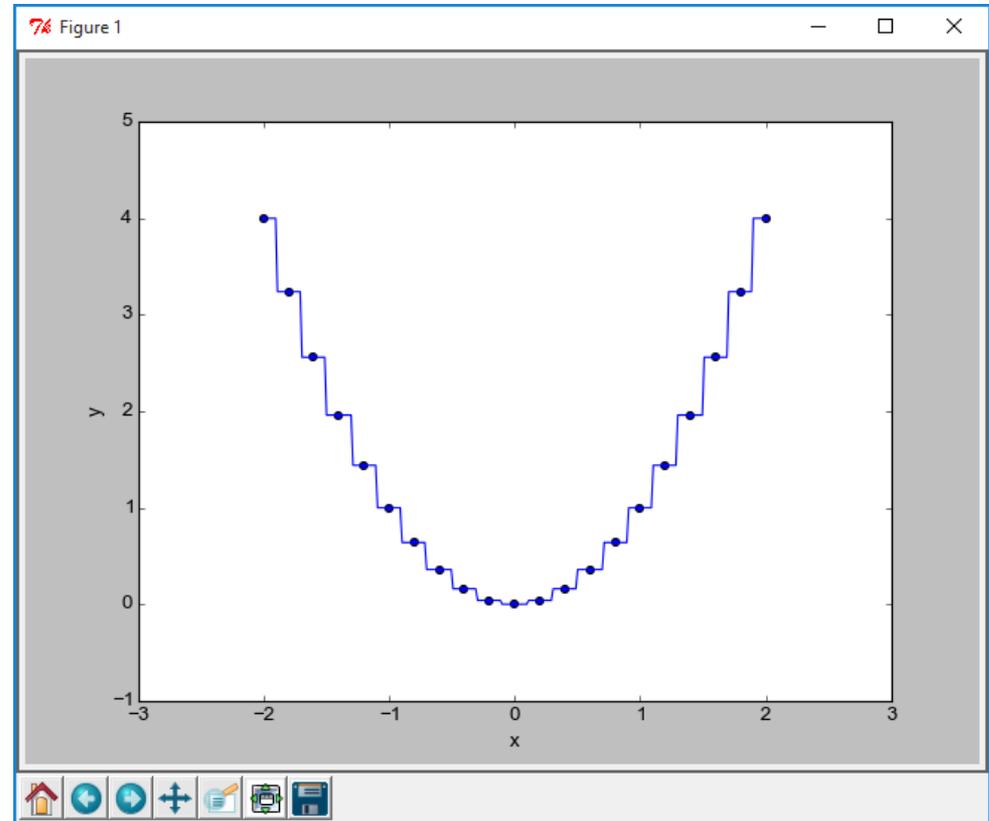


# INTERPOLATION

Given a simple function:

```
funct1 =  
interpolate.interp1d(  
    xvals, yvals,  
    kind='nearest'  
)
```

Nearest Neighbour  
interpolation

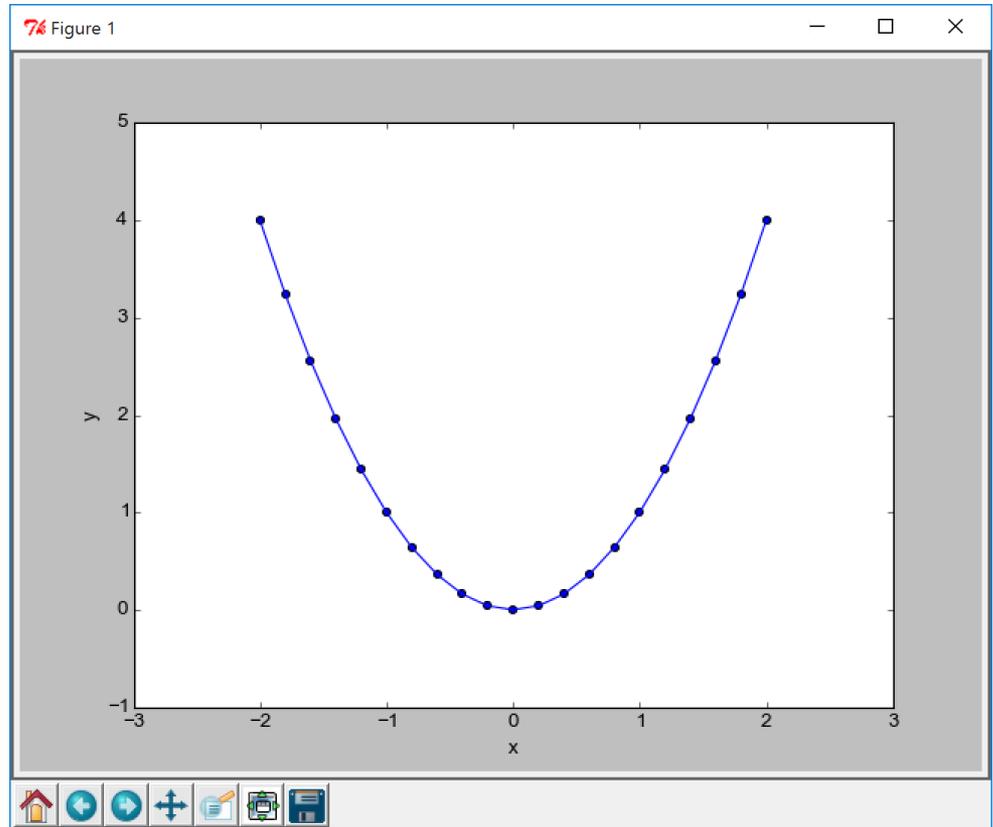


# INTERPOLATION

Given a simple function:

```
funct1 =  
interpolate.interp1d(  
    xvals, yvals,  
    kind='linear'  
)
```

Linear interpolation

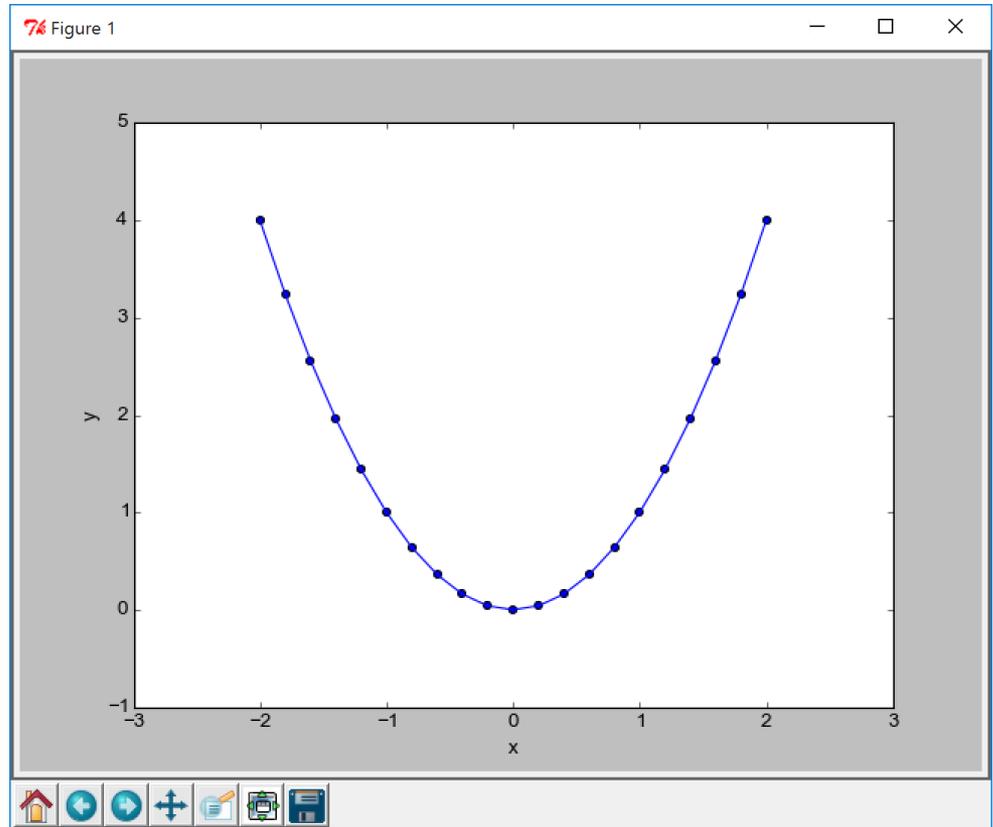


# INTERPOLATION

Given a simple function:

```
funct1 =  
interpolate.interp1d(  
    xvals, yvals,  
    kind='slinear'  
)
```

Linear Spline  
(first order)



# NDIMAGE

Library of functions useful for dealing with N-dimensional images. In particular, we'll be using the filters for smoothing. Also includes functions to interpolate and manipulate images. Importing the library:

```
from scipy import ndimage
```

Includes basic filters:

```
ndimage.gaussian_filter(...)  
ndimage.median_filter(...)
```

Or using generic convolution:

```
ndimage.convolve(...)
```

# NDIMAGE

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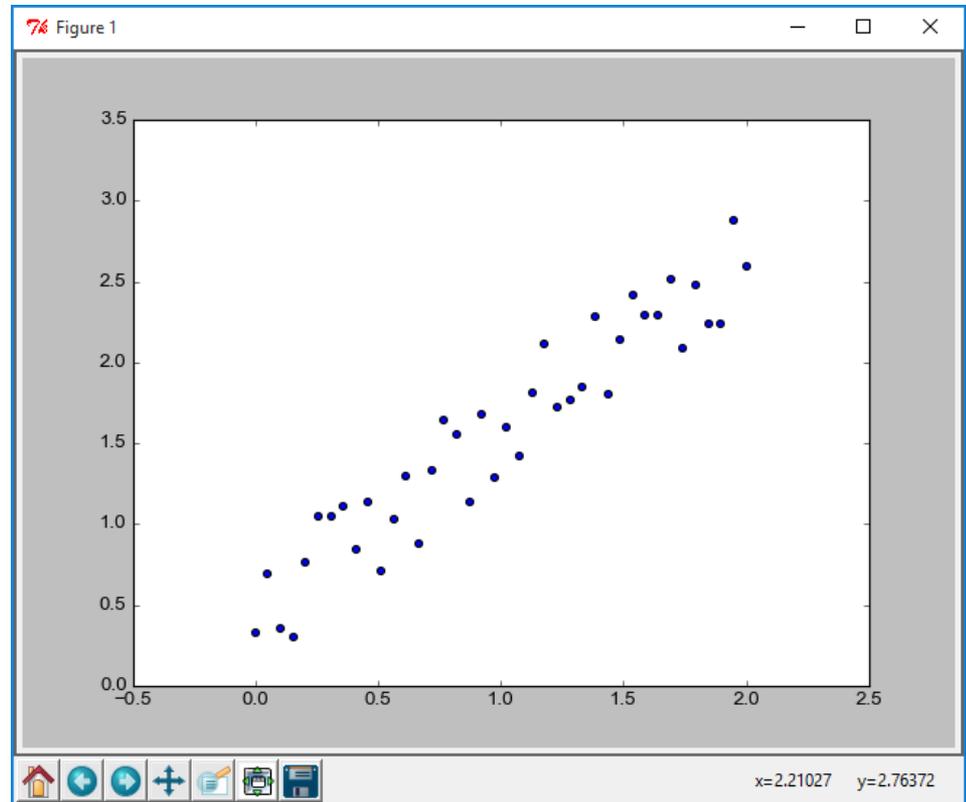
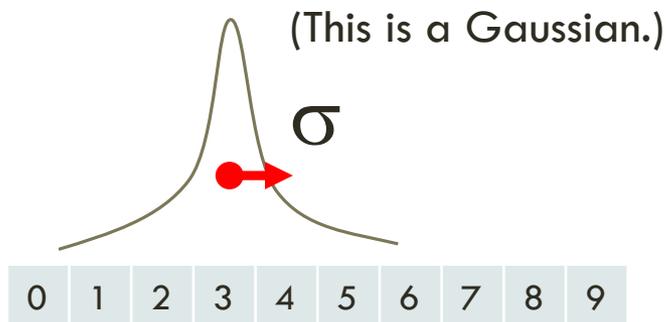
## PRO TIP:

These functions work just as well on 2-D or 3-D arrays as they do on 1-D arrays.

# SMOOTHING/FILTERING

Given an array:

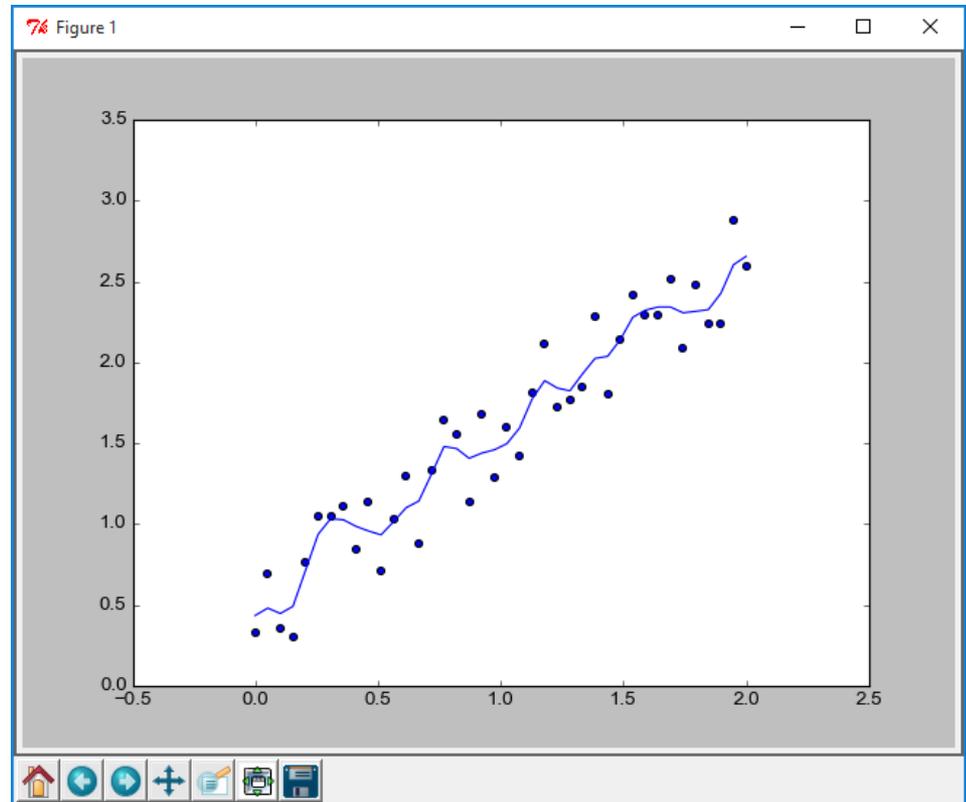
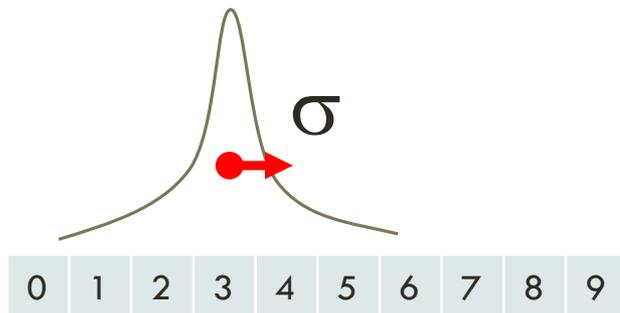
```
ndimage.gaussian_filter(  
arr1, sigma=1.0)
```



# SMOOTHING/FILTERING

Given an array:

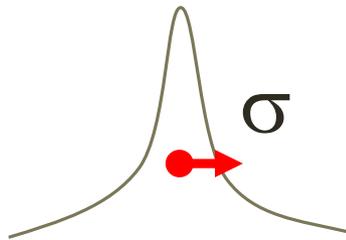
```
ndimage.gaussian_filter(  
arr1, sigma=1.0)
```



# SMOOTHING/FILTERING

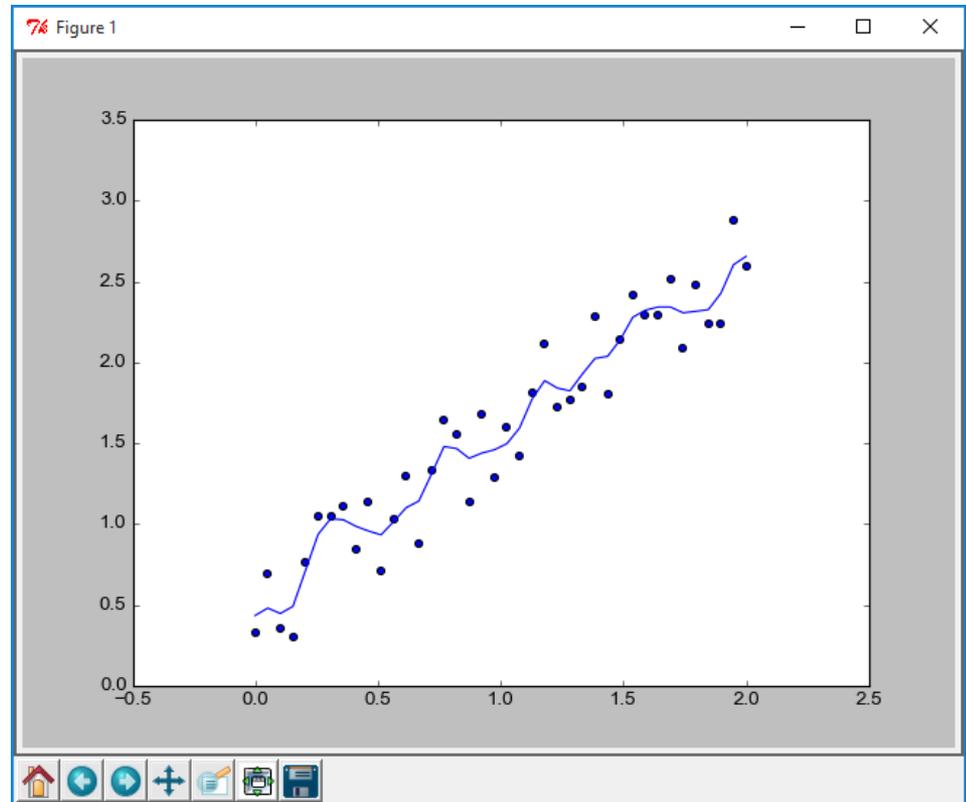
Given an array:

```
ndimage.gaussian_filter(  
arr1, sigma=1.0)
```



**PRO TIP:**

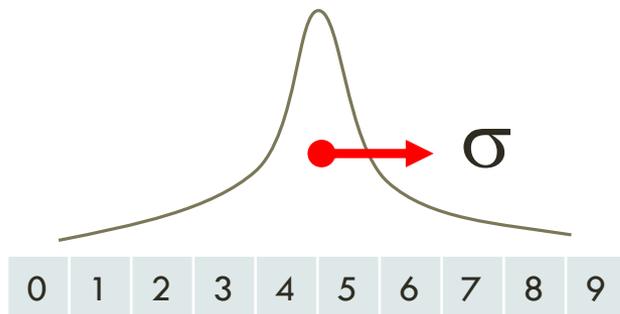
Values in the filter are in pixel units.



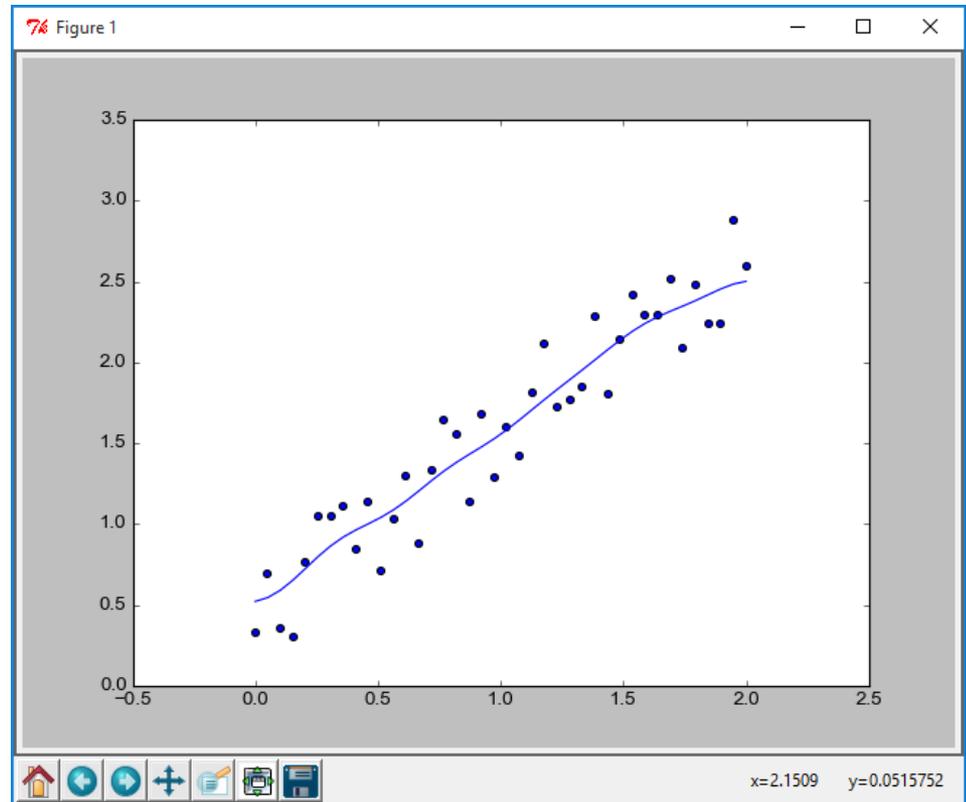
# SMOOTHING/FILTERING

Given an array:

```
ndimage.gaussian_filter(  
arr1, sigma=3.0)
```



(This is also a Gaussian.  
I can draw in PowerPoint)

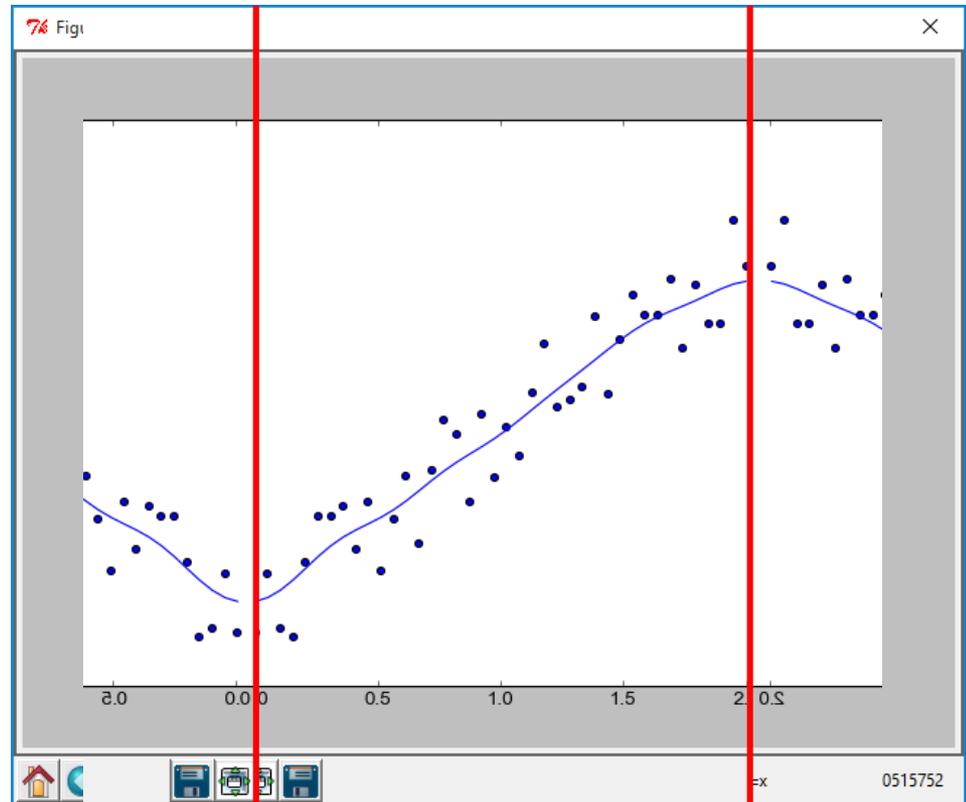


# SMOOTHING/FILTERING

Given an array:

```
ndimage.gaussian_filter(  
arr1, sigma=3.0,  
mode='reflect')
```

The “mode” of the filtering indicates what happens at the edges of the dataset. “Reflect” treats the edges of the domain as the inverse of the dataset.

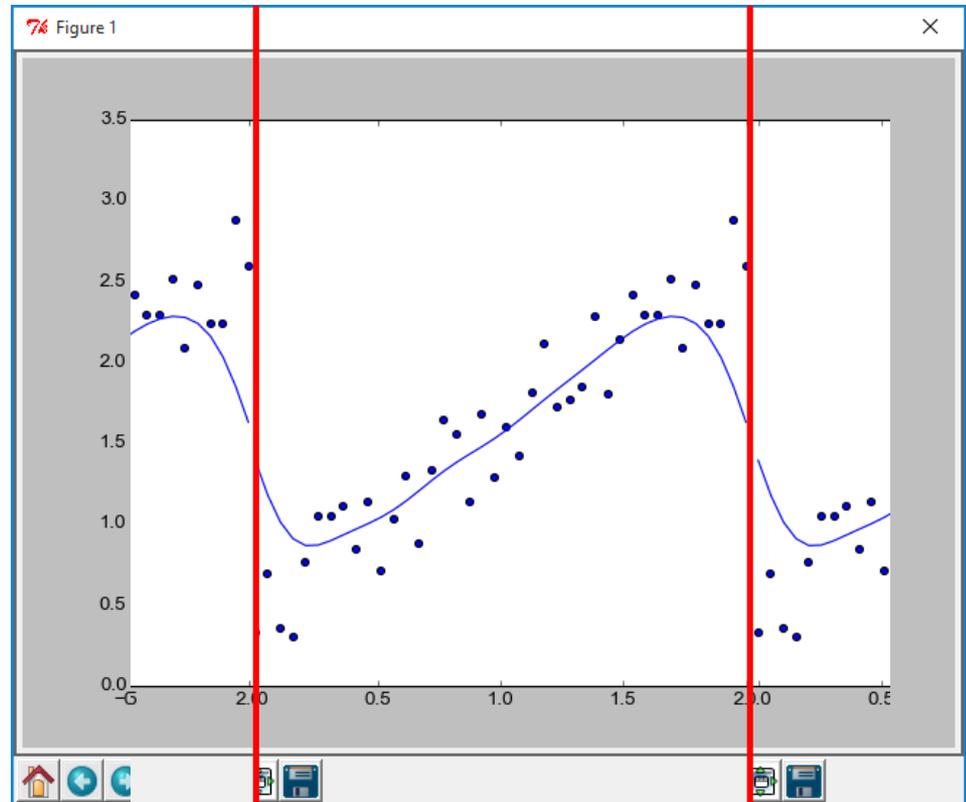


# SMOOTHING/FILTERING

Given an array:

```
ndimage.gaussian_filter(  
arr1, sigma=3.0,  
mode='wrap')
```

“Wrap” treats the data like a tiled patchwork, with the data repeating itself on either end.



# INTEGRATION

Importing the Functions:

```
from scipy import integrate
```

Functions that integrate fixed samples (i.e., numpy arrays):

```
integrate.cumtrapz(...) # Composite trapezoidal  
integrate.simps(...) # Simpson's Rule  
integrate.romb(...) # Romberg integration
```

Functions that integrate functions:

```
integrate.quad(...) # General Purpose Integration  
integrate.nquad(...) # Multiple Variable  
integrate.quadrature(...) # Fixed Tolerance Integration
```

# INTEGRATION

Composite Trapezoidal (Cumulative)

```
intarr = integrate.cumtrapz(yarr, x=xarr)
```

This function returns an array (size one less than original array). To get the final integrated value of the entire array:

```
total = intarr[-1]
```

# INTEGRATION

Composite Trapezoidal (Cumulative)

```
intarr = integrate.cumtrapz(yarr, x=xarr)
```

This function returns an array (size one less than original array). To get the final integrated value of the entire array:

```
total = intarr[-1]
```

## PRO TIP:

This also works when an array isn't evenly spaced. Just make sure to pass an array of x values.

# INTEGRATION

Integrating functions (using quad):

```
# Creating function to integrate:  
funct1 = lambda x: x**2  
  
# Integrating the function over range [min, max]  
total, err = integrate.quad(funct1, min, max)
```

Can integrate from negative infinity to positive infinity through:

```
total, err = integrate.quad(funct1, -np.inf, np.inf)
```

# STATISTICS

Importing the Functions:

```
from scipy import stats
```

Provides access to a variety of useful functions:

```
stats.mode(arr1) # Modal Value
```

```
# Statistical measures
```

```
stats.skew(arr1), stats.kurtosis(arr1), ...
```

```
# Trimmed Mean, Standard Deviation
```

```
stats.tmean(arr1, limits=[min, max]), stats.tstd(...)
```

```
# Percentile -> Score
```

```
stats.scoreatpercentile(arr1, percentile)
```

# OPTIMIZE/FITTING

Importing the Functions:

```
from scipy import optimize
```

Unlike the other operations, curve fitting is **quite complex**. Consequently, there are a number of different functions and algorithms available to handle any number of situations. **Be sure that the fitting method you're using is doing what you think it is.**

The basic functions you should know about:

```
optimize.curve_fit(...) # Fit a defined curve to data
```

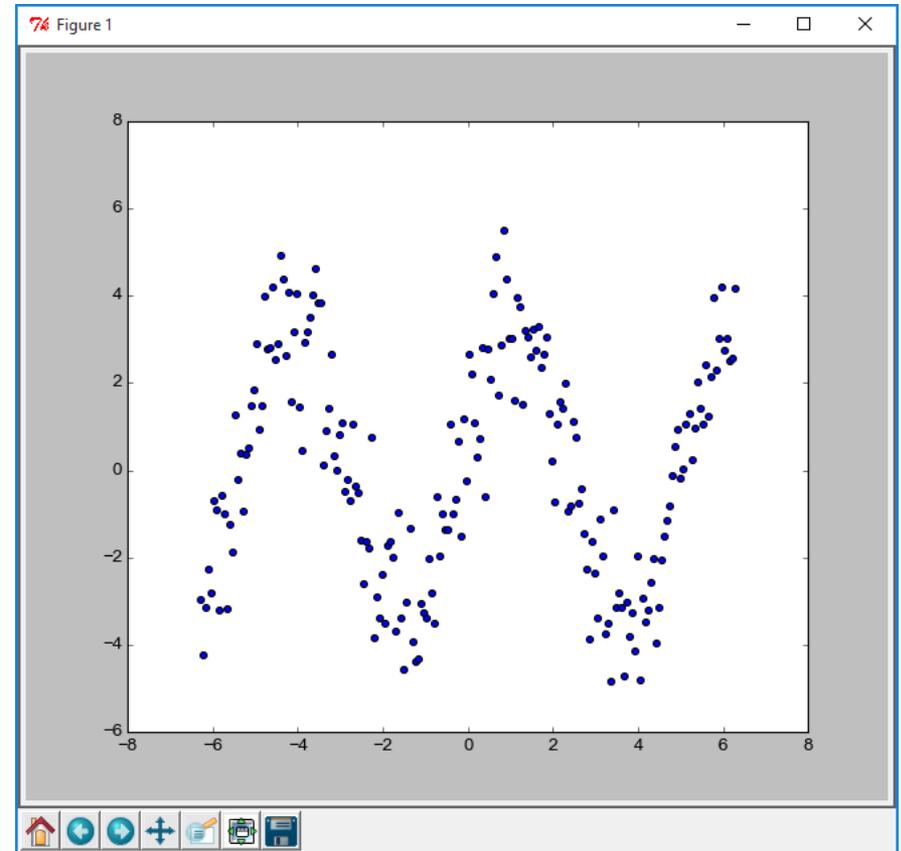
```
# Minimized the sum of square of an equation  
optimize.leastsq(...)
```

```
optimize.minimize(...) # Minimize a function
```

# OPTIMIZE/FITTING

Basic curve fitting, using `curve_fit`:

```
# Function to fit to:  
funct1 = lambda x,a,b,c:  
    a*np.sin(b*x + c)
```



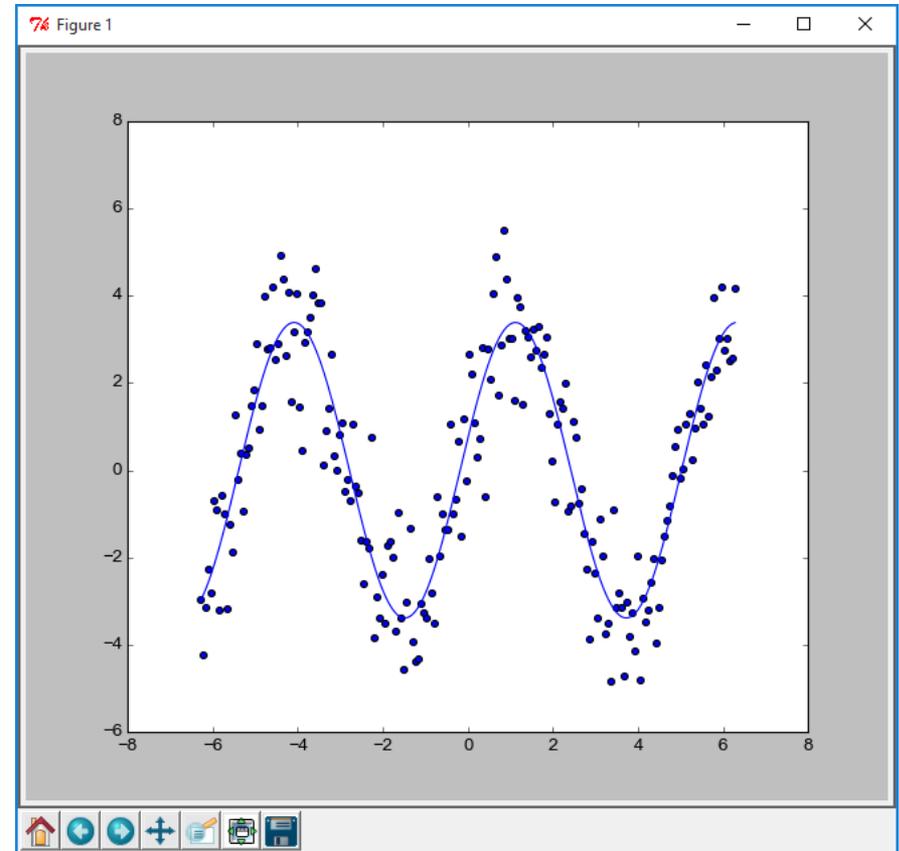
# OPTIMIZE/FITTING

Basic curve fitting, using `curve_fit`:

```
# Function to fit to:  
funct1 = lambda x,a,b,c:  
    a*np.sin(b*x + c)
```

Assuming data in arrays named `data_x` and `data_y`:

```
# Fitting the data:  
param, covar =  
optimize.curve_fit(  
    funct1, data_x, data_y  
)
```



# OPTIMIZE/FITTING

We can use the “minimize” function to be more flexible for fitting, minimizing the “least-square” function:

$$\sum (data - model)^2$$

Or if there are errors that you want to weight the fitting by:

$$\sum \left( \frac{data - model}{error} \right)^2$$

Both of these functions are always positive (for real numbers), and minimizing them ensures that you have adopted the best-fit parameters

# OPTIMIZE/FITTING

Taking the equation from earlier:

$$y = a \sin(bx + c)$$

Which converts into:

```
funct1 = lambda x,a,b,c: a*np.sin(b*x + c)
```

# OPTIMIZE/FITTING

Taking the equation from earlier:

$$y = a \sin(bx + c)$$

Which converts into:

```
funct1 = lambda x,a,b,c: a*np.sin(b*x + c)
```

We can create a (single variable) function to minimize:

```
funct2 = lambda par:  
    np.sum((data_y - funct1(data_x, *par))**2)
```

Or with errors:

```
funct2 = lambda par:  
    np.sum(((data_y - funct1(data_x, *par))/err)**2)
```

# OPTIMIZE/FITTING

Taking the equation from earlier:

$$y = a \sin(bx + c)$$

Which converts into:

```
funct1 = lambda x,a,b,c: a*np.sin(b*x + c)
```

We can create a (single variable) function to minimize:

```
funct2 = lambda par: funct1(data_x, *par)**2)
```

## PRO TIP:

If you have a tuple, list, or array that contains all the parameters you want to pass to a function in order, you can pass it by using the asterisk (\*).

```
funct1(data_x, *par)/err)**2)
```

# OPTIMIZE/FITTING

Taking the equation from earlier:

$$y = a \sin(bx + c)$$

Which converts into:

```
funct1 = lambda x,a,b,c: a*np.sin(b*x + c)
```

We can create a (single variable) function to minimize:

```
funct2 = lambda par:
```

```
    funct1(data_x, *par)**2)
```

## PRO TIP 2:

Notice that the minimizing functions have only one argument, which is a 1-D vector of the required parameters.

```
    (funct1(data_x, *par)/err)**2)
```

# OPTIMIZE/FITTING

Piecing this into the `minimize_scalar` function:

```
result = optimize.minimize(func2, x0=initialguess)
```

The initial guess is an array with the same size as the parameters you want to fit.

This function abstracts a variety of different algorithms with different possible parameters. For instance you can use the following to define bounds for the fitting:

```
result = optimize.minimize(  
    func2, x0=initialguess, method='L-BFGS-B',  
    bounds=((0, 5), (0, 2), (0,3))  
)
```

# OPTIMIZE/FITTING

Once you have the result, you have lots of information provided to you as a dictionary:

```
result['x'] # The final parameters of the fit
result['success'] # Whether the fit was successful
result['nit'] # Number of Iterations Performed
result['jac'] # The jacobian of the fit
```

# OPTIMIZE/FITTING

Once you have the result, you have lots of information provided to you as a dictionary:

```
result['x'] # The final parameters of the fit
result['success'] # Whether the fit was successful
result['nit'] # Number of Iterations Done
result['jac'] # The jacobian
```

## PRO TIP:

When fitting, especially this way, check to ensure convergence.

**EXERCISE TIME!**

Hello from the outside.